

17. Let L_1 be the distance from the closer speaker to the listener. The distance from the other speaker to the listener is $L_2 = \sqrt{L_1^2 + d^2}$, where d is the distance between the speakers. The phase difference at the listener is $\phi = 2\pi(L_2 - L_1)/\lambda$, where λ is the wavelength.

For a minimum in intensity at the listener, $\phi = (2n + 1)\pi$, where n is an integer. Thus $\lambda = 2(L_2 - L_1)/(2n + 1)$. The frequency is

$$f = \frac{v}{\lambda} = \frac{(2n + 1)v}{2(\sqrt{L_1^2 + d^2} - L_1)} = \frac{(2n + 1)(343 \text{ m/s})}{2(\sqrt{(3.75 \text{ m})^2 + (2.00 \text{ m})^2} - 3.75 \text{ m})} = (2n + 1)(343 \text{ Hz}).$$

Now $20,000/343 = 58.3$, so $2n + 1$ must range from 0 to 57 for the frequency to be in the audible range. This means n ranges from 0 to 28.

(a) The lowest frequency that gives minimum signal is ($n = 0$) $f_{\min,1} = 343 \text{ Hz}$.

(b) The second lowest frequency is ($n = 1$) $f_{\min,2} = [2(1) + 1]343 \text{ Hz} = 1029 \text{ Hz} = 3f_{\min,1}$. Thus, the factor is 3.

(c) The third lowest frequency is ($n = 2$) $f_{\min,3} = [2(2) + 1]343 \text{ Hz} = 1715 \text{ Hz} = 5f_{\min,1}$. Thus, the factor is 5.

For a maximum in intensity at the listener, $\phi = 2n\pi$, where n is any positive integer. Thus $\lambda = (1/n)(\sqrt{L_1^2 + d^2} - L_1)$ and

$$f = \frac{v}{\lambda} = \frac{nv}{\sqrt{L_1^2 + d^2} - L_1} = \frac{n(343 \text{ m/s})}{\sqrt{(3.75 \text{ m})^2 + (2.00 \text{ m})^2} - 3.75 \text{ m}} = n(686 \text{ Hz}).$$

Since $20,000/686 = 29.2$, n must be in the range from 1 to 29 for the frequency to be audible.

(d) The lowest frequency that gives maximum signal is ($n = 1$) $f_{\max,1} = 686 \text{ Hz}$.

(e) The second lowest frequency is ($n = 2$) $f_{\max,2} = 2(686 \text{ Hz}) = 1372 \text{ Hz} = 2f_{\max,1}$. Thus, the factor is 2.

(f) The third lowest frequency is ($n = 3$) $f_{\max,3} = 3(686 \text{ Hz}) = 2058 \text{ Hz} = 3f_{\max,1}$. Thus, the factor is 3.